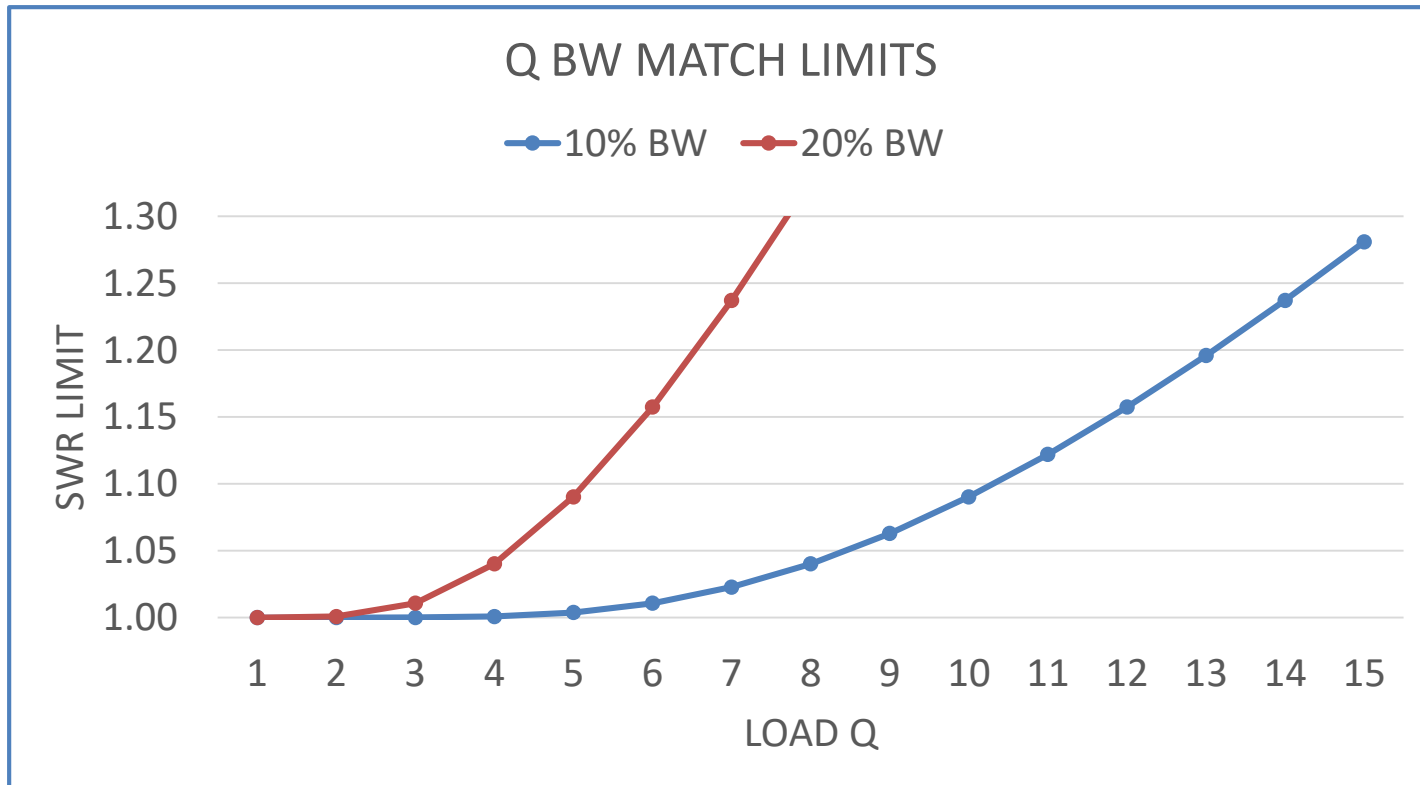


IMPEDANCE MATCHING TECHNIQUES FOR RF & MICROWAVE CIRCUIT DESIGN

2019 Microwave Update

ACHIEVABLE MATCH DEPENDS ON Q_L AND BW%

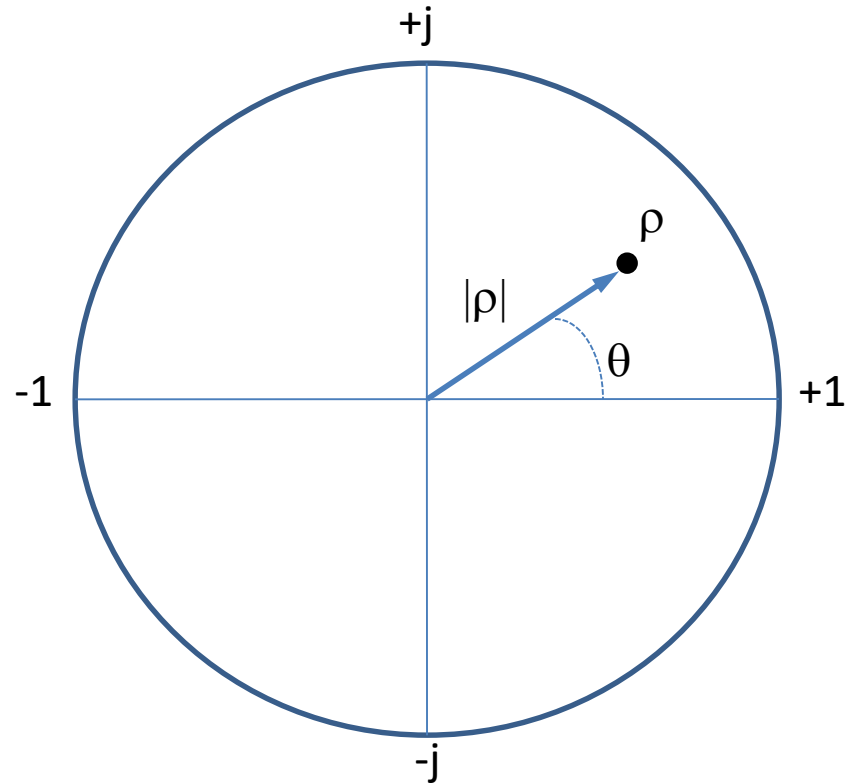
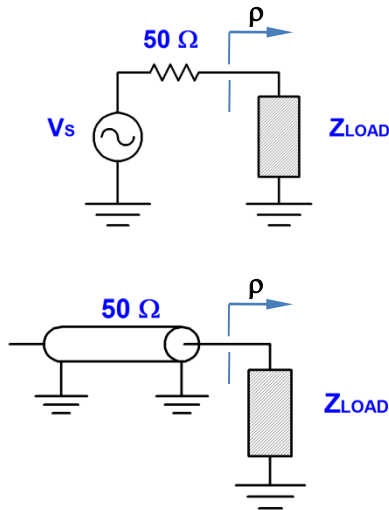


$$\rho \geq e^{\left(\frac{-\pi}{Q*BW}\right)}$$

$$SWR = (1 + \rho)/(1 - \rho)$$

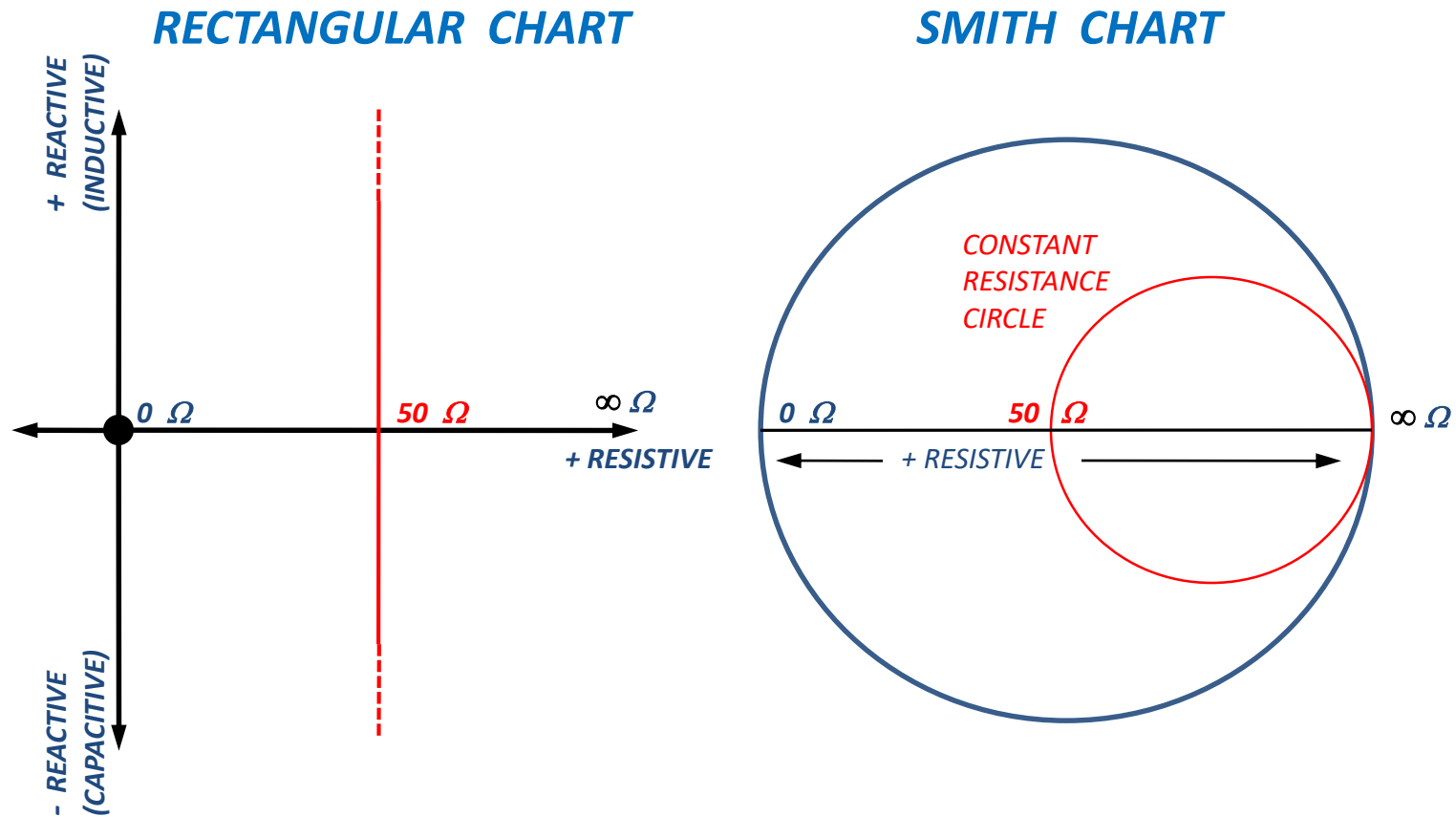
ORIGIN OF THE SMITH CHART

REFLECTION COEFFICIENT: ρ



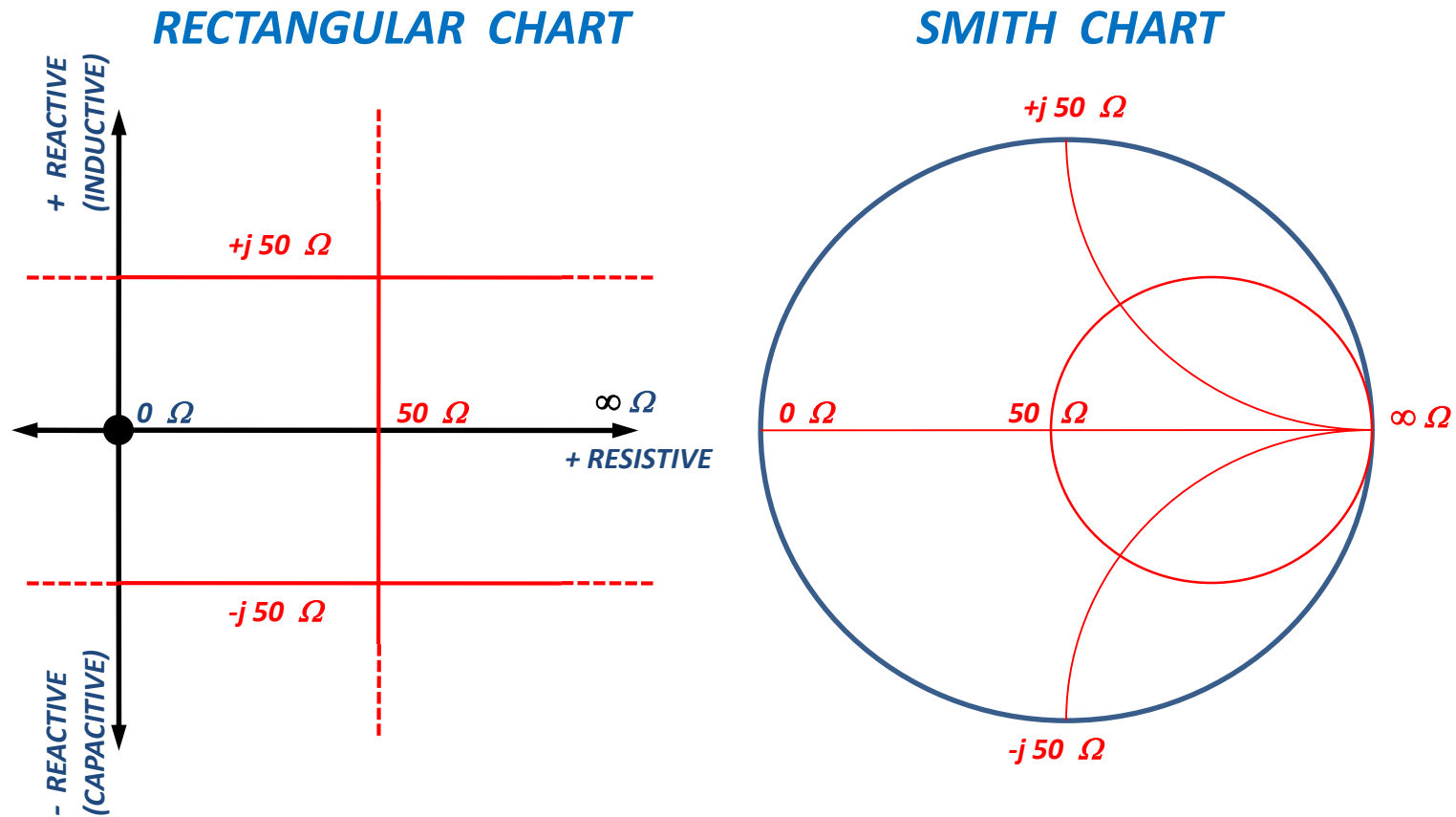
- ρ IS RATIO OF REFLECTED TO FORWARD VOLTAGE AT LOAD
- ρ IS COMPLEX NUMBER: (REAL, IMAGINARY) or (MAGNITUDE, ANGLE)
- $|\rho| = 1.0$ IS MAXIMUM POSSIBLE WITH PASSIVE LOAD (TOTAL REFLECTION)
- $|\rho| = 1.0$ CIRCLE IS OUTER BOUNDARY OF STANDARD SMITH CHART

IMPEDANCE VIEW – CONSTANT RESISTANCE



- $Z = R + jX$
- IMPEDANCE HAS A **REAL PART** AND AN **IMAGINARY PART**
- IMPEDANCE REPRESENTS A SERIES CONNECTION
- CONSTANT **REAL LINES** BECOME **CIRCLES** ON SMITH CHART

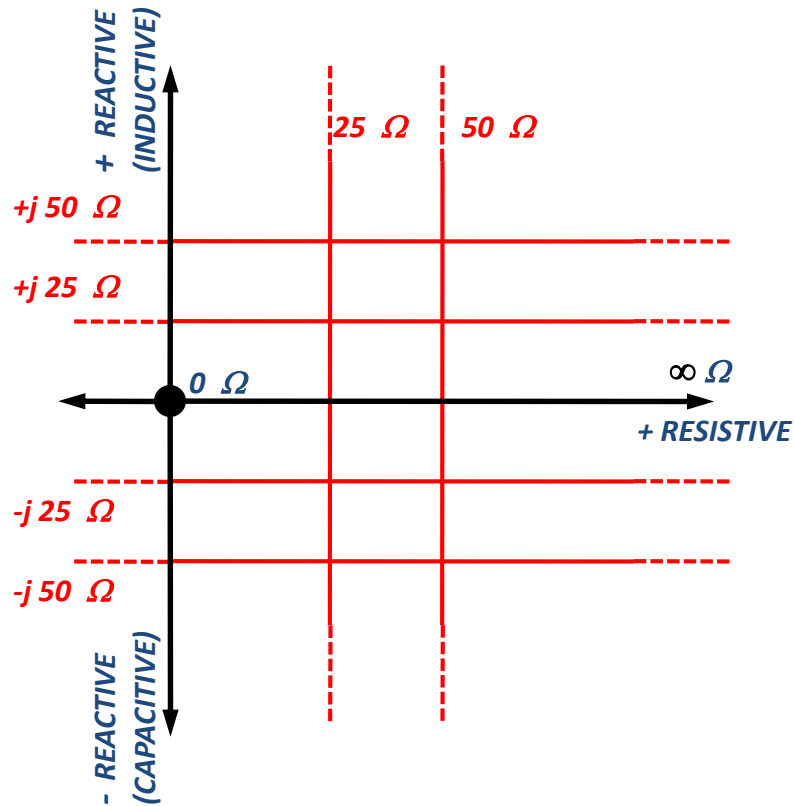
IMPEDANCE VIEW – CONSTANT REACTANCE



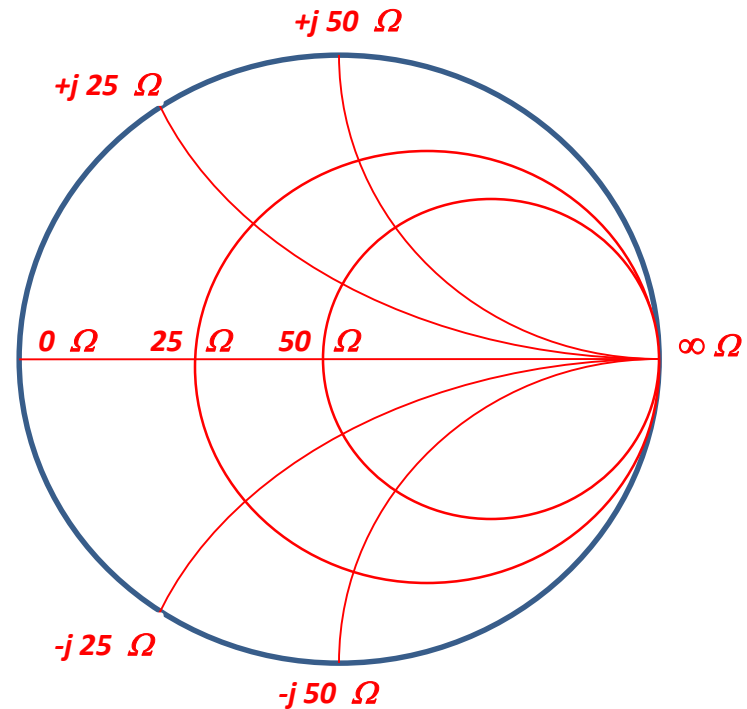
- CONSTANT **REACTANCE LINES** BECOME **ARCS** ON SMITH CHART
- UPPER HALF IS INDUCTIVE
- LOWER HALF IS CAPACITIVE
- POSITIVE REAL IS **INSIDE** THE SMITH UNIT CIRCLE

IMPEDANCE VIEW

RECTANGULAR CHART



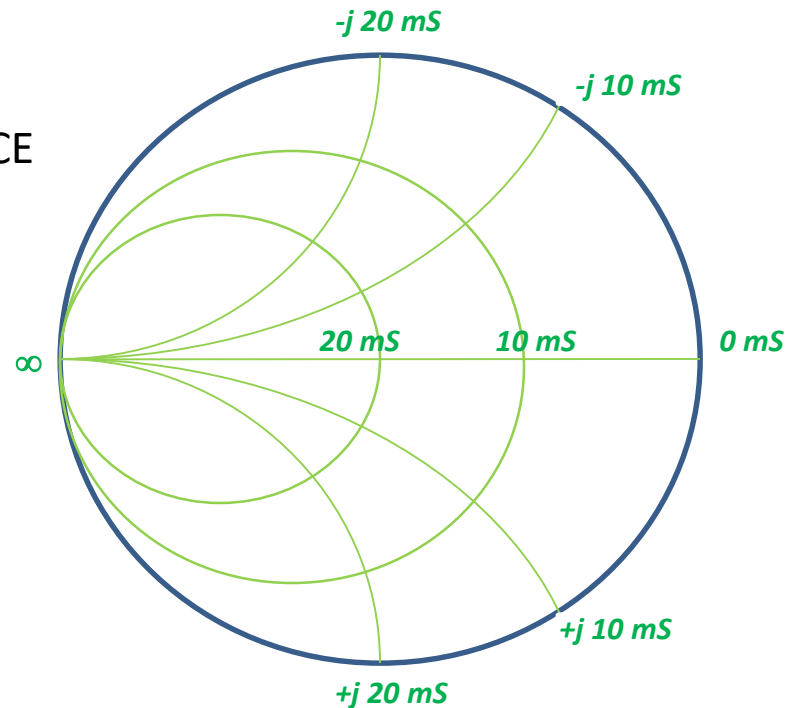
SMITH CHART



- IMPEDANCE REPRESENTATION OF THE SMITH CHART
- USUALLY IN RED
- LOWER HALF IS CAPACITIVE
- POSITIVE REAL IS **INSIDE** THE SMITH UNIT CIRCLE

ADMITTANCE VIEW

- $Y = 1/Z = G + jB$
- ADMITANCE IS RECIPROCAL IMPEDANCE
- ADMITANCE REPRESENTS A PARALLEL CONNECTION

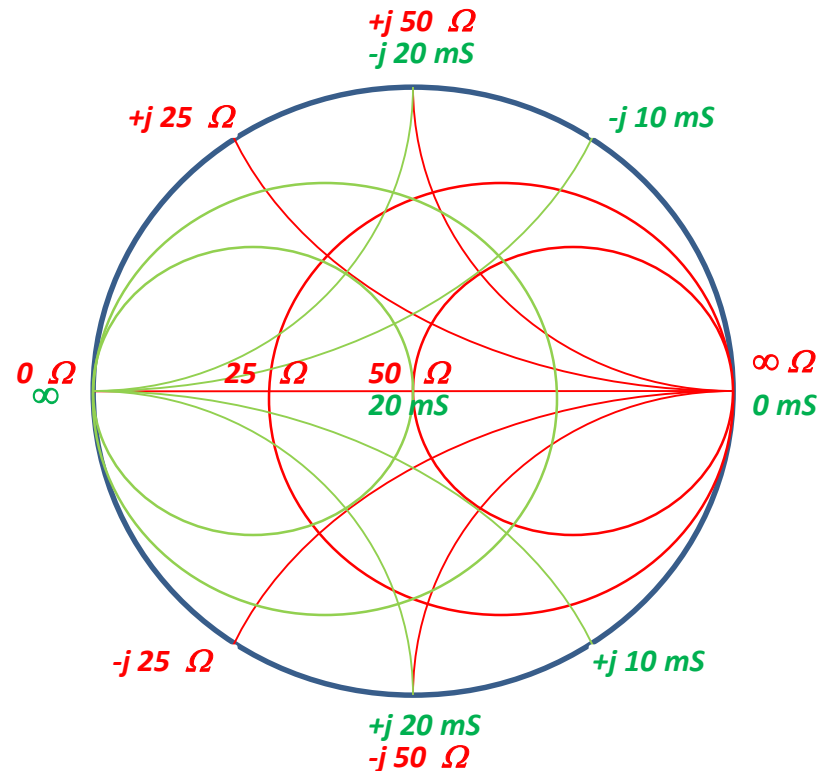


- ADMITANCE HAS A REAL PART (CONDUCTANCE) AND AN IMAGINARY PART (SUSCEPTANCE)
- CONSTANT CONDUCTANCE IS A CIRCLE ON SMITH CHART
- CONSTANT SUSCEPTANCE IS AN ARC ON SMITH CHART

OVERLAY SMITH CHART

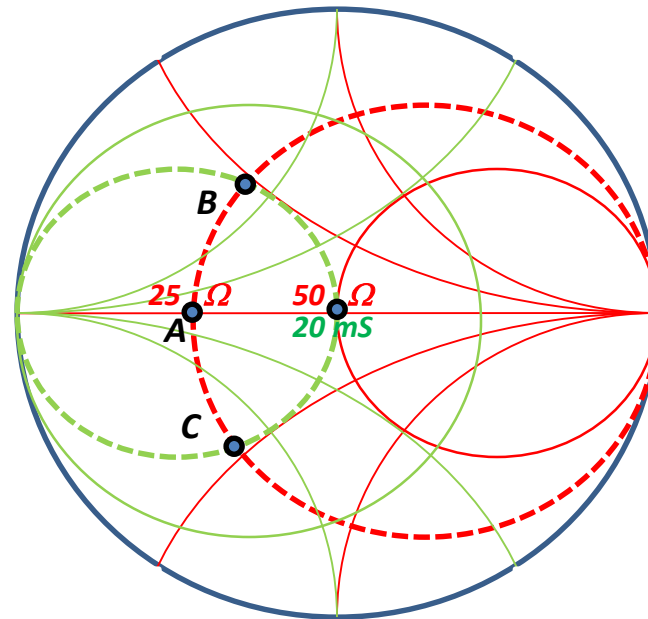
- BOTH IMPEDANCE AND ADMITTANCE VIEWS OF SAME POINT
- SIMULTANEOUS VIEW OF **SERIES IMPEDANCE** OR **PARALLEL ADMITTANCE**
- THIS VIEW PROVIDES A CONVENIENT WAY TO DESIGN LUMPED ELEMENT MATCHING NETWORKS
- DOWNLOAD A NORMALIZED CHART:

http://k5tra.net/TechFiles/smith_color.pdf



LUMPED ELEMENT Z-MATCHING

- A SIMPLE EXAMPLE IS TO MATCH BETWEEN 25Ω AND 50Ω
- FROM THE 25Ω POINT (**A**) WE FIRST USE THE IMPEDANCE VIEW TO MOVE TO EITHER POINT **B** OR **C**
- **A**, **B**, and **C** ARE ALL ON THE CONSTANT 25Ω CIRCLE
- THE (+) REACTIVE SHIFT FROM **A** TO **B** REPRESENTS A SERIES INDUCTOR
- THE (-) REACTIVE SHIFT FROM **A** TO **C** REPRESENTS A SERIES CAPACITOR
- NOTE THAT BOTH **B** and **C** ARE ON THE 20 mS CIRCLE. THIS ALLOWS US TO REACH 50Ω WITH A SHUNT ELEMENT



- THROUGH **B** REQUIRES SERIES INDUCTOR AND SHUNT CAPACITOR
- THROUGH **C** REQUIRES SERIES CAPACITOR AND SHUNT INDUCTOR

L OR C VALUES FROM CHART

- SERIES L OR C ELEMENT VALUES ARE CALCULATED FROM REACTANCE SHIFTS ALONG A CONSTANT RESISTANCE CIRCLE:

- $L_S = \frac{|X_L|}{2\pi F}$ and $C_S = \frac{1000}{2\pi F |X_C|}$,

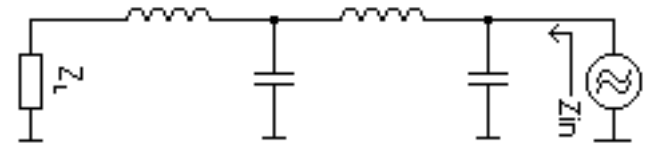
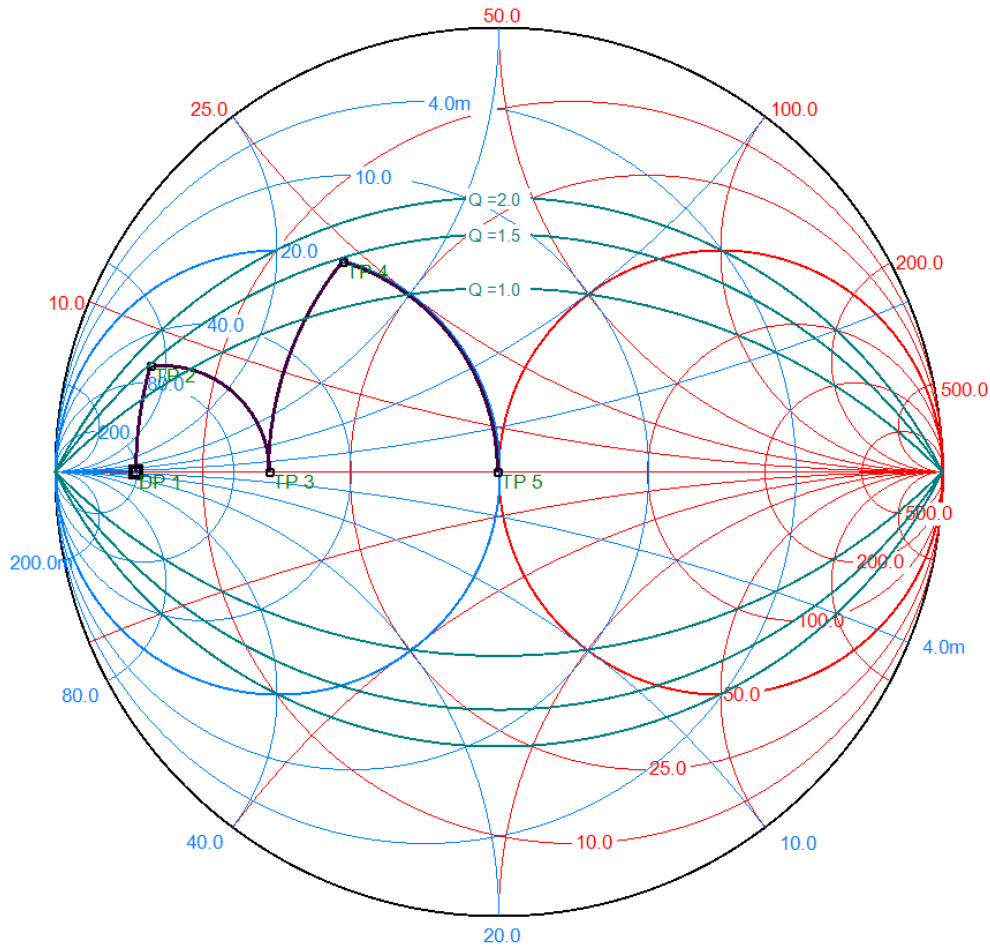
units are L(nH), C(pF), X(Ω) and F(GHz).

- SHUNT L OR C ELEMENT VALUES ARE CALCULATED FROM SUSCEPTANCE SHIFT ALONG A CONSTANT CONDUCTANCE CIRCLE:

- $C_P = \frac{|B_C|}{2\pi F}$ and $L_P = \frac{1000}{2\pi F |B_L|}$,

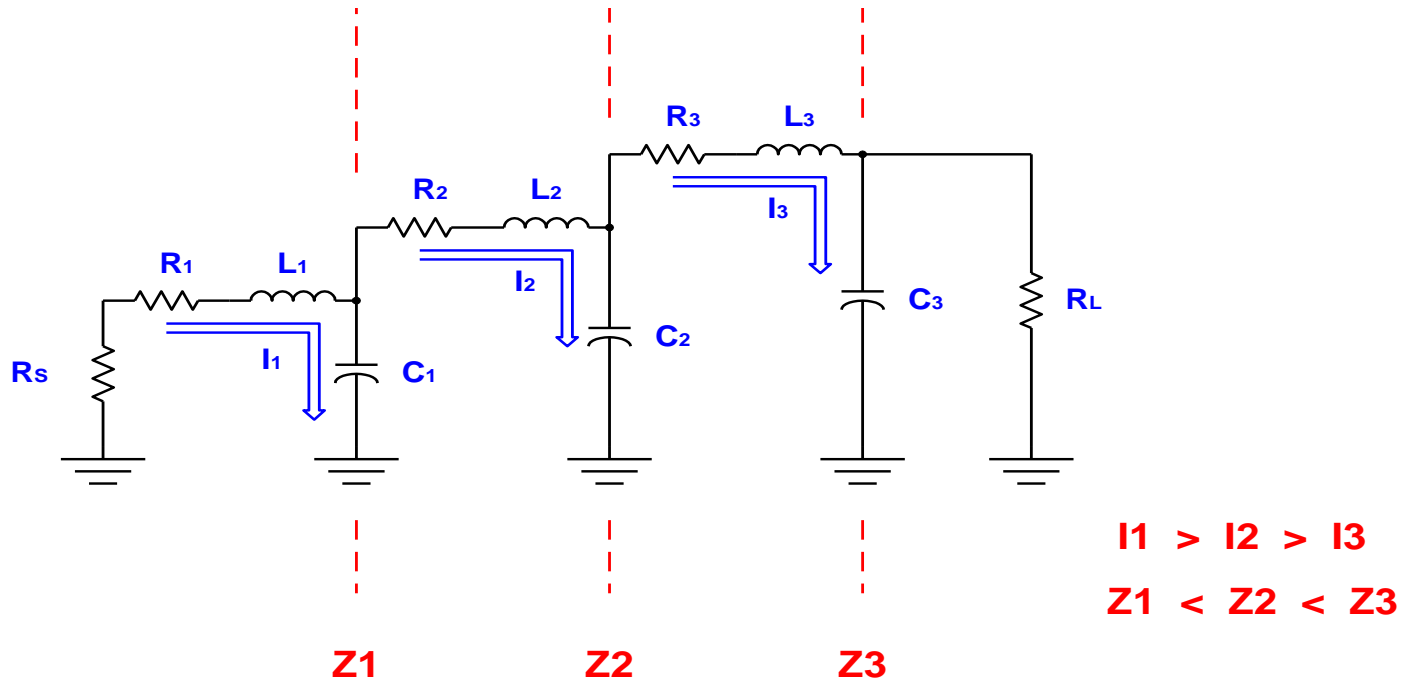
units are L(nH), C(pF), B(mS) and F(GHz).

Ls Cp Ls Cp LOWPASS MATCH



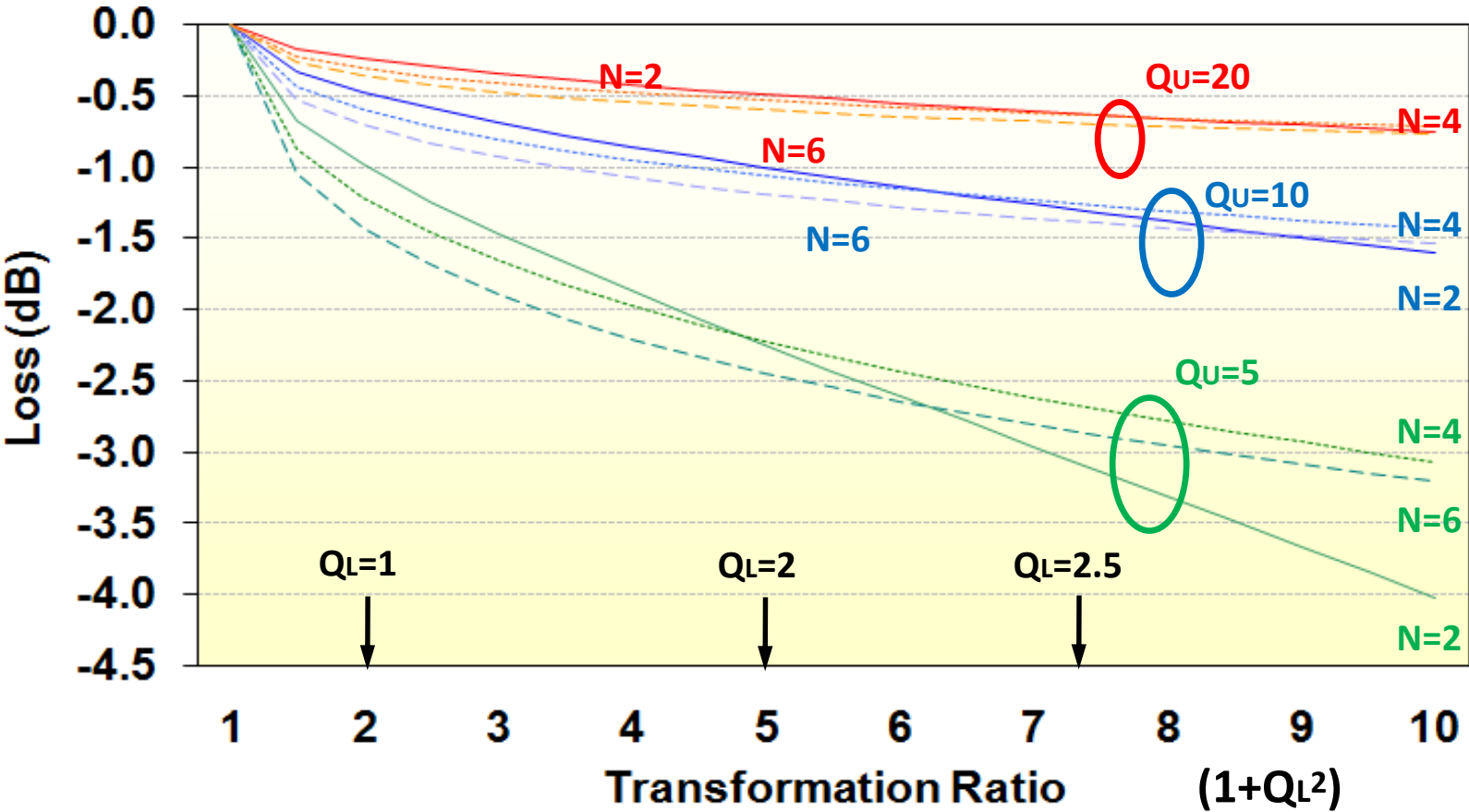
$(5.00 + j0.00) \Omega @ 1.3 \text{ GHz}$
 900.0 pH
 11.5 pF
 2.9 nH
 3.6 pF

LOSS CONSIDERATIONS



- POWER TRANSFER OF EACH SECTION IS: $(Q_U - Q_L) / Q_U$
- $I^2 R$ LOSSES (PRIMARILY IN INDUCTORS) PRODUCE INSERTION LOSS
- Z TRANSFORMATION PER SECTION IS: $1 + Q_L^2$

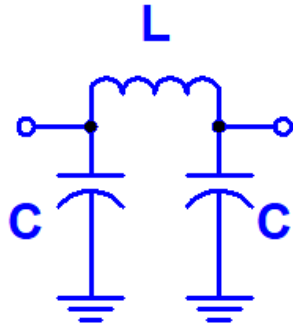
NUMBER OF ELEMENTS - LOSS TRADE-OFF



LUMPED DESIGN ON A CIRCUIT BOARD

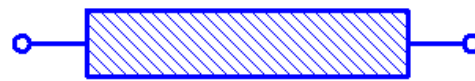
- THERE REALLY ARE NO LUMPED ELEMENTS
 - CHIP CAPACITORS HAVE SERIES INDUCTANCE (and LOSS)
 - CHIP INDUCTORS HAVE DISTRIBUTED CAPACITANCE (SELF RESONANCE)
 - CHIP RESISTORS HAVE SERIES INDUCTANCE AND SHUNT CAPACITANCE
- CIRCUIT BOARD TRACES OVER BACKSIDE GROUND ARE MICROSTRIP TRANSMISSION LINES.
- MICROSTRIP LINES ARE QUASI-TEM; SO THEY CAN BE REPRESENTED AS A SERIES OF INCREMENTAL SERIES L AND SHUNT C ELEMENTS.
- $Z_0 = \sqrt{\frac{L}{C}}$, WHERE L AND C ARE INCREMENTAL (PER UNIT LENGTH)
- THIN TRACES:
 - HIGH Z_0 TRACES HAVE HIGH L/C
 - USED FOR PRINTED INDUCTORS
- WIDE TRACES:
 - LOW Z_0 TRACES HAVE MORE C
 - PROVIDE SHUNT C (AND SOME SERIES L)

LC REPRESENTATION OF A SHORT LINE

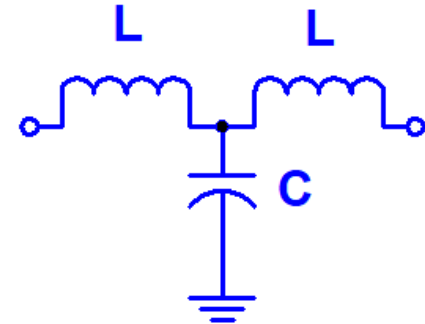


$$X_L = Z_0 \cdot \sin(\beta l)$$

$$X_C = Z_0 \cdot \cot(\beta l / 2)$$



$$Z_0, \quad \theta = \beta l$$



$$X_L = Z_0 \cdot \tan(\beta l / 2)$$

$$X_C = \frac{Z_0}{\sin(\beta l)}$$

- HIGH Z_0 LINES USE THE π CIRCUIT FOR INDUCTOR REPRESENTATION
- THE END CAPACITANCES ARE SMALL WITH HIGH Z_0 LINES
- LOW Z_0 LINES USE THE T CIRCUIT FOR CAPACITOR REPRESENTATION
- THE END INDUCTANCES ARE SMALL WITH LOW Z_0 LINES

LUMPED EQUIVALENT CALCULATOR

MicroStrip Lumped Equivalent Circuits

Length 300 Analysis 20.00 Width

C(pF)-T 0.4304 Synth. T Synth. Pi 4.3345 L(nH)-Pi

L(nH)-T 2.2388 microns mils 0.2299 C(pF)-Pi

ApelSoft

Solve Microstrip About

100.36 3.020 0.5755 20.59

Impedance Effective Dielectric Relative Velocity Phase Length (degrees)

4.500 50.00 1.000 1.296

Dielectric Constant Dielectric Thickness Conductor Thickness Frequency (GHz)

- MICROSTRIP ANALYSIS AND SYNTHESIS
- π and T EQUIVALENT CIRCUIT CALCULATION
- SELECTABLE UNITS: MILS OR MICRONS

<http://k5tra.net/TechFiles/LumpEquiv.exe>

SMD CHIP SERIES INDUCTANCE

SMD SERIES INDUCTANCE

| CHIP PKG | DIM (mil ²) | L(nH) |
|----------|-------------------------|-------|
| 0402 | 40x20 | 0.59 |
| 0603 | 60x30 | 0.77 |
| 0805 | 80x50 | 0.84 |
| ATC 100A | 55x55 | 0.55 |
| ATC 100B | 110x110 | 0.77 |

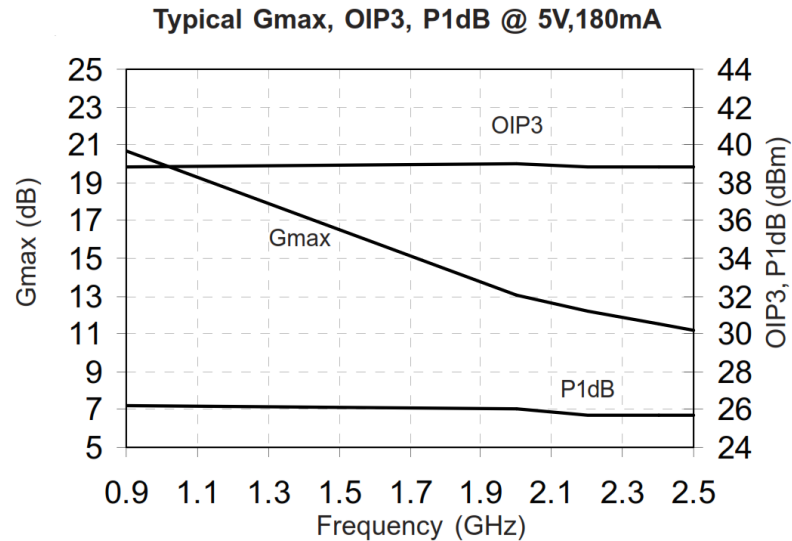
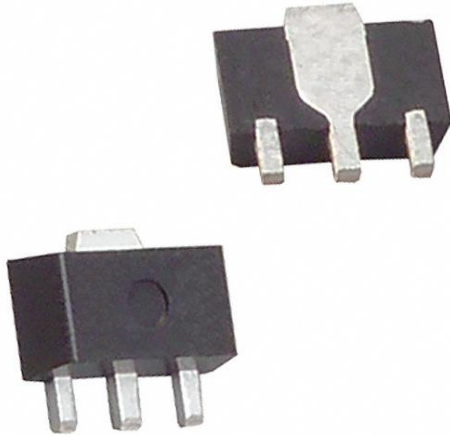
Series Trap

| | | | | | |
|------------|-------|-----------------|---------------------|---------|---------|
| Freq (GHz) | 1.296 | Harmonics | Fo | 2 Fo | 3 Fo |
| Ls (nH) | 0.77 | Effective Value | 1.30 | 2.59 | 3.89 |
| Cs (pF) | 3.0 | Type | 3.54 pF | 7.75 pF | 0.21 nH |
| | | | Cap | Cap | Ind |
| Calculate | | | Resonant Freq (GHz) | 3.31 | |

<http://k5tra.net/TechFiles/SeriesTrap.exe>

- AN 0603 3 pF CAP ALSO HAS 0.77 nH SERIES INDUCTANCE
- SERIES RESONANT FREQUENCY IS 3.31 GHz
- EFFECTIVE CAPACITANCE IS 3.54 AT 1296 MHz
- EFFECTIVE CAPACITANCE IS 7.75 AT 2nd HARMONIC OF 1296 MHz
- EFFECTIVE INDUCTANCE IS 0.21 nH AT 3rd HARMONIC OF 1296 MHz

DESIGN EXAMPLE: SGA-9189 PA DRIVER



- THE SGA-9189 IS A MEDIUM POWER SiGe TRANSISTOR
- > 25 dBm POWER OUTPUT AT $V_{cc} = +5V$
- SOT-89 PACKAGE
- MANUFACTURER: RFMD

SGA-9189 TARGET IMPEDANCES

- OPTIMUM EXTERNAL IMPEDANCES at 1296 MHz :

$$Z_{S\text{ OPT}} = 7.1 - j 4.4 \Omega$$

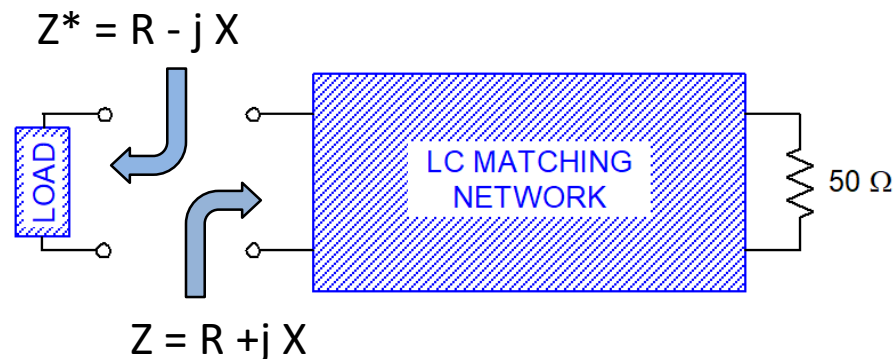
$$Z_{L\text{ OPT}} = 18.4 + j 4.1 \Omega$$

- OPTIMUM MATCHING NETWORKS WILL PROVIDE A MATCH TO LOADS THAT ARE COMPLEX CONJUGATE OF THE OPTIMUMS

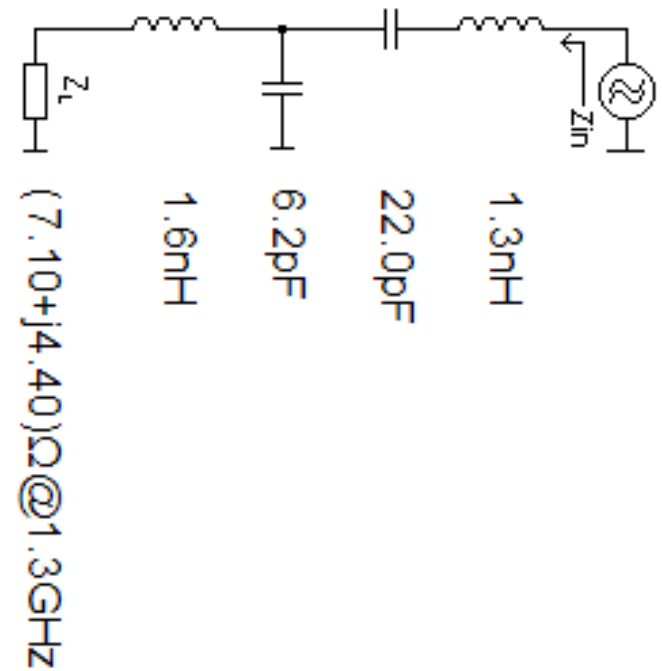
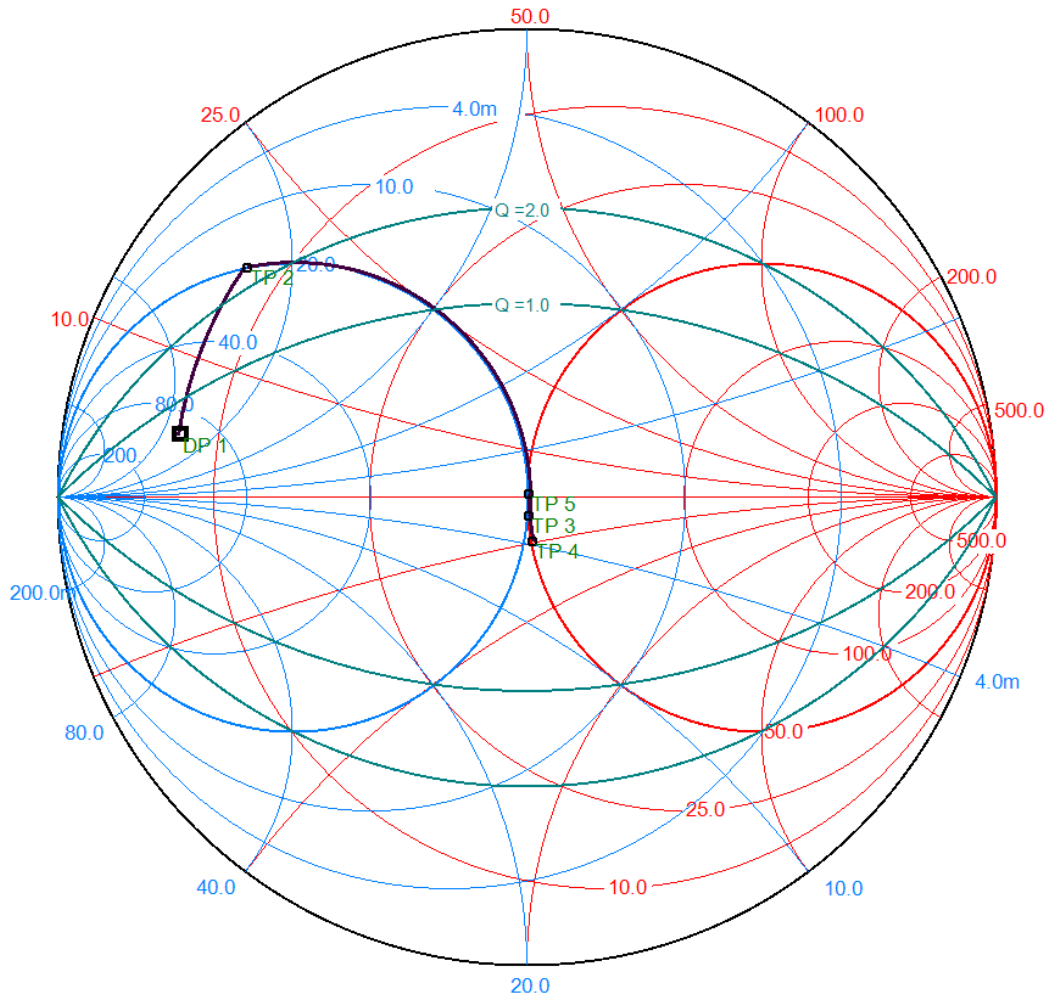
- SO, DESIGN MATCHING NETWORKS TERMINATED WITH:

$$Z_{S\text{ OPT}}^* = 7.1 + j 4.4 \Omega$$

$$Z_{L\text{ OPT}}^* = 18.4 - j 4.1 \Omega$$



SGA-9189 LC INPUT MATCH



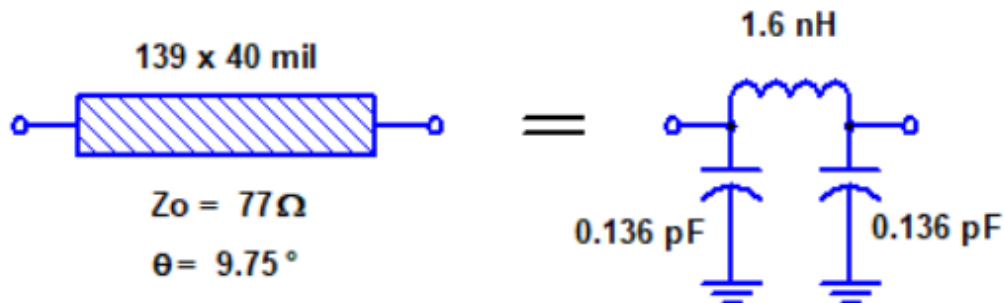
1.6 nH FROM 77 Ω MICROSTRIP

MicroStrip Lumped Equivalent Circuits

| | | | | | |
|---------|--------|---|-----------|----------|----------|
| Length | 139.19 | Analysis | 40.00 | Width | |
| C(pF)-T | 0.2703 | Synth. T | Synth. Pi | 1.6000 | L(nH)-Pi |
| L(nH)-T | 0.8058 | <input type="radio"/> microns <input checked="" type="radio"/> mils | 0.1361 | C(pF)-Pi | |

ApelSoft

| | | | |
|---------------------|----------------------|---------------------|------------------------|
| Solve Microstrip | About | | |
| 76.94 | 3.144 | 0.5640 | 9.75 |
| Impedance | Effective Dielectric | Relative Velocity | Phase Length (degrees) |
| 4.500 | 50.00 | 1.000 | 1.296 |
| Dielectric Constant | Dielectric Thickness | Conductor Thickness | Frequency (GHz) |



6.2 pF SHUNT CAP

SMD SERIES INDUCTANCE

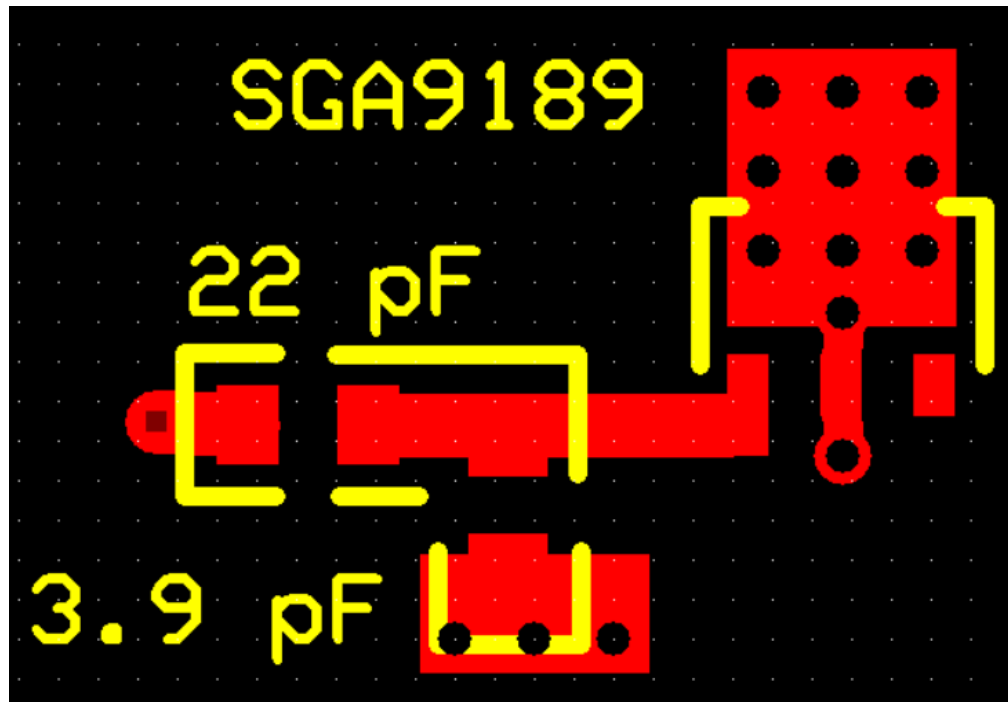
| CHIP PKG | DIM (mil ²) | L(nH) |
|----------|-------------------------|-------|
| 0402 | 40x20 | 0.59 |
| 0603 | 60x30 | 0.77 |
| 0805 | 80x50 | 0.84 |
| ATC 100A | 55x55 | 0.55 |
| ATC 100B | 110x110 | 0.77 |

Series Trap

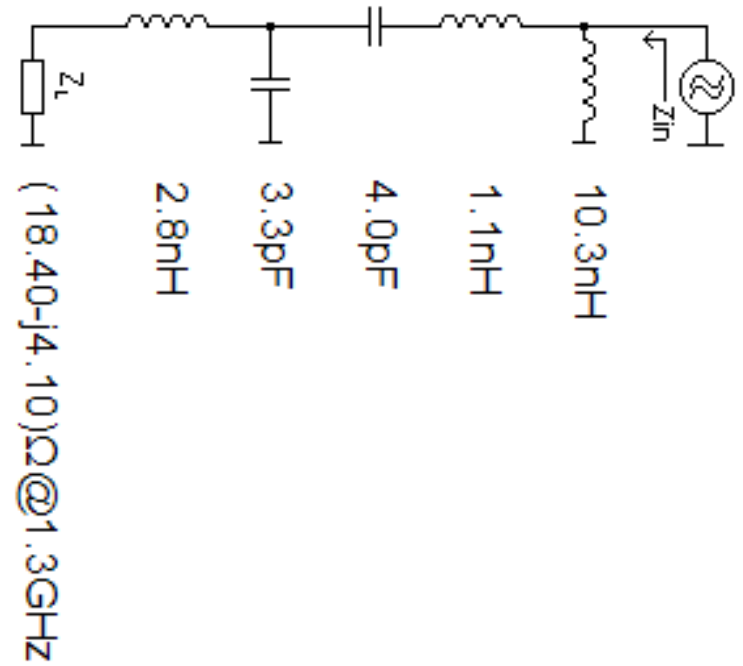
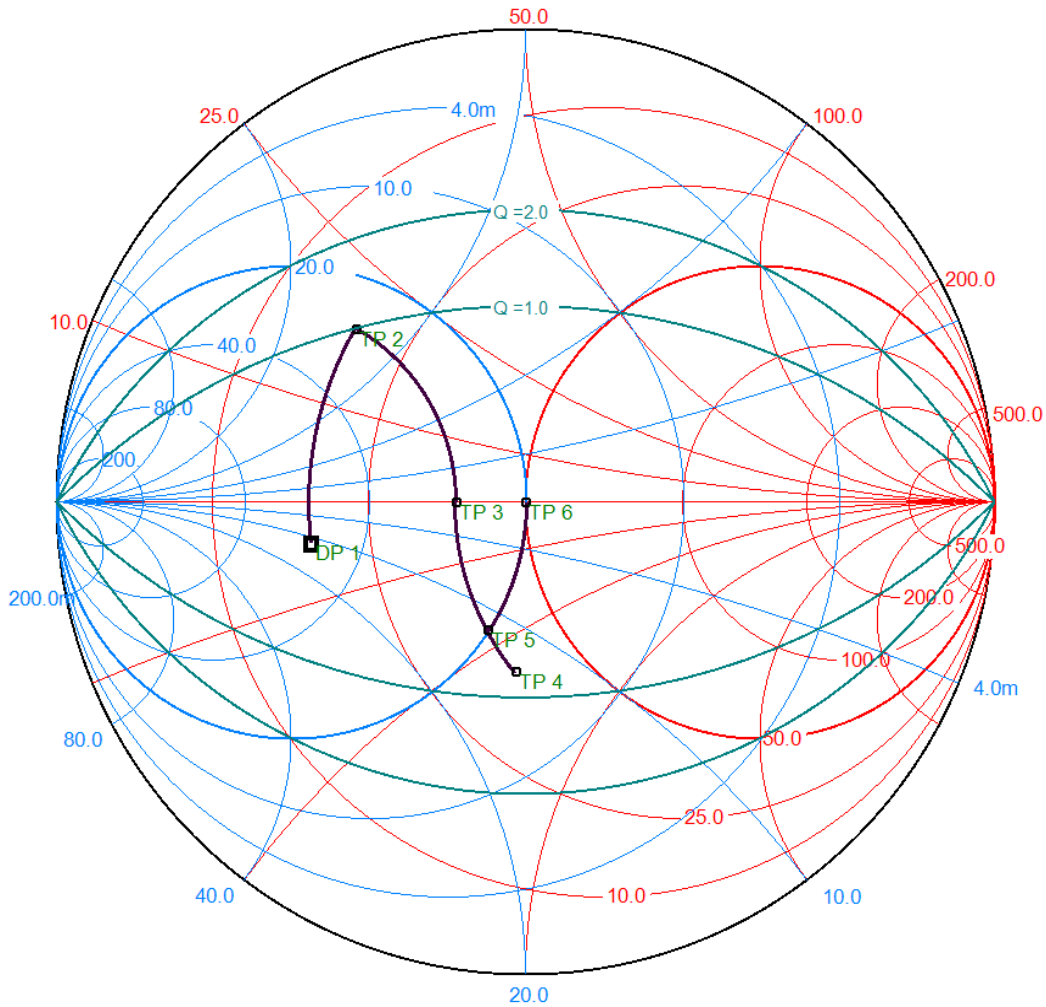
| | | | | | |
|------------|-------|---------------------|---------|---------|---------|
| Freq (GHz) | 1.296 | Harmonics | Fo | 2 Fo | 3 Fo |
| Ls (nH) | 1.4 | Effective Value | 1.30 | 2.59 | 3.89 |
| Cs (pF) | 3.9 | Type | 6.11 pF | 0.43 nH | 0.97 nH |
| | | | Cap | Ind | Ind |
| Calculate | | Resonant Freq (GHz) | | | 2.15 |

- 0805 SMD 3.9 pF CHIP HAS 0.84 nH IN SERIES
- THE PATH TO GROUND IS A 0.035 DIAMETER VIA = 0.52 nH
- THE TOTAL SERIES INDUCTANCE IS 1.4 nH (= 0.84 + 0.52 nH)
- EFFECTIVE CAPACITANCE IS 6.1 pF AT 1296 MHz
- THE TOTAL SHUNT C IS 6.23 pF (= 6.1 + 0.13 pF)

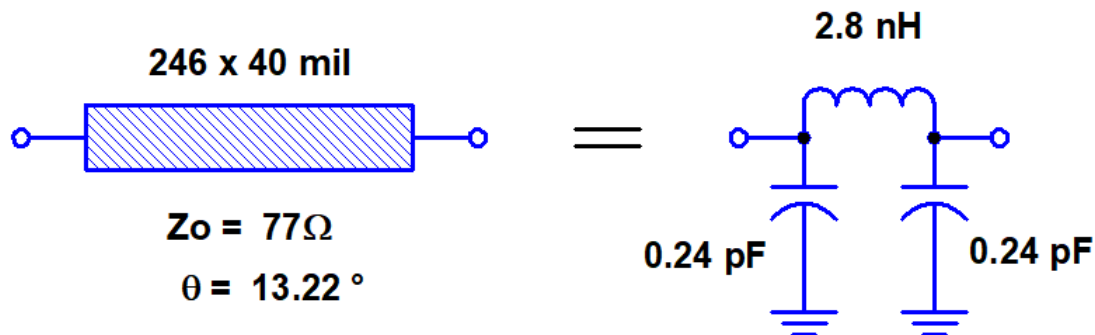
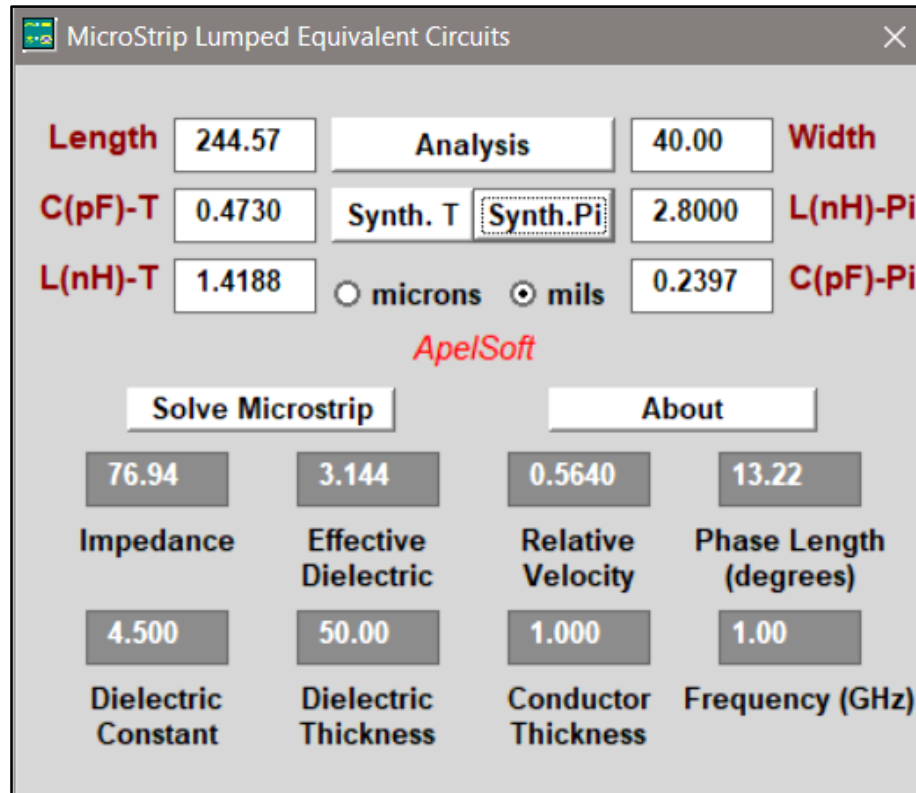
INPUT MATCH ON 50 MIL FR4



SGA-9189 LC OUTPUT MATCH



2.8 nH FROM 77 Ω MICROSTRIP



3.3 pF SHUNT CAP

SMD SERIES INDUCTANCE

| CHIP PKG | DIM (mil ²) | L(nH) |
|----------|-------------------------|-------|
| 0402 | 40x20 | 0.59 |
| 0603 | 60x30 | 0.77 |
| 0805 | 80x50 | 0.84 |
| ATC 100A | 55x55 | 0.55 |
| ATC 100B | 110x110 | 0.77 |

Series Trap

| | | | | | |
|------------|-------|-----------------|---------------------|----------|---------|
| Freq (GHz) | 1.296 | Harmonics | Fo | 2 Fo | 3 Fo |
| Ls (nH) | 1.4 | Effective Value | 1.30 | 2.59 | 3.89 |
| Cs (pF) | 2.4 | Type | 3.09 pF | 22.06 pF | 0.70 nH |
| Calculate | | | Cap | Cap | Ind |
| | | | Resonant Freq (GHz) | 2.75 | |

- 0805 SMD 2.4 pF CHIP HAS 0.84 nH IN SERIES
- THE PATH TO GROUND IS A 0.035 DIAMETER VIA = 0.52 nH
- THE TOTAL SERIES INDUCTANCE IS 1.4 nH (= 0.84 + 0.52 nH)
- EFFECTIVE CAPACITANCE IS 3.09 pF AT 1296 MHz
- THE TOTAL SHUNT C IS 3.3 pF (= 3.09 + 0.24 pF)

4.0 pF SERIES CAP

SMD SERIES INDUCTANCE

| CHIP PKG | DIM (mil ²) | L(nH) |
|----------|-------------------------|-------|
| 0402 | 40x20 | 0.59 |
| 0603 | 60x30 | 0.77 |
| 0805 | 80x50 | 0.84 |
| ATC 100A | 55x55 | 0.55 |
| ATC 100B | 110x110 | 0.77 |

- 0805 SMD 4 pF CHIP HAS 0.84 nH IN SERIES
- THE LUMPED DESIGN HAS PROVIDED 1.1 nH IN SERIES WITH 4 pF
- THE EXCESS 0.26 nH (=1.1 – 0.84 nH) REPRESENTS 22 MILS of 77 Ω LINE

10.3 nH SHUNT INDUCTOR

MicroStrip Lumped Equivalent Circuits

Length: 470.57 Analysis: 10.00 Width: **Width**

C(pF)-T: 0.5356 Synth. T: Synth.Pi L(nH)-Pi: 8.1500

L(nH)-T: 4.2675 microns mils C(pF)-Pi: 0.2804

ApelSoft

Solve Microstrip About

| | | | |
|---------------------|----------------------|---------------------|------------------------|
| 123.36 | 2.924 | 0.5848 | 24.53 |
| Impedance | Effective Dielectric | Relative Velocity | Phase Length (degrees) |
| 4.500 | 50.00 | 1.000 | 1.00 |
| Dielectric Constant | Dielectric Thickness | Conductor Thickness | Frequency (GHz) |

Shunt Trap

| | Fo | 2 Fo | 3 Fo |
|------------|-------|---------|---------|
| Freq (GHz) | 1.296 | 2.59 | 3.89 |
| Lp (nH) | 8.67 | 24.3 nH | 0.09 pF |
| Cp (pF) | 0.28 | Ind | Cap |

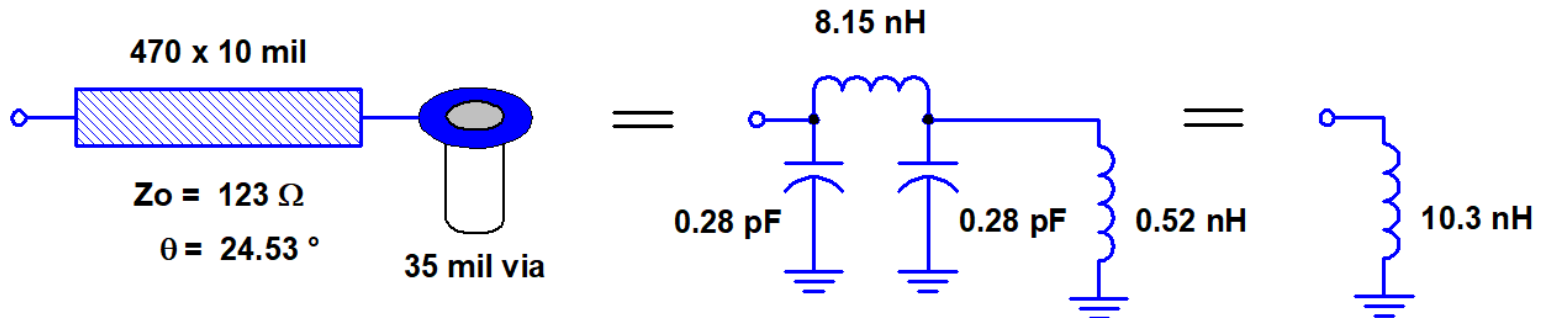
Harmonics: 1.30, 2.59, 3.89

Effective Value: 10.3 nH

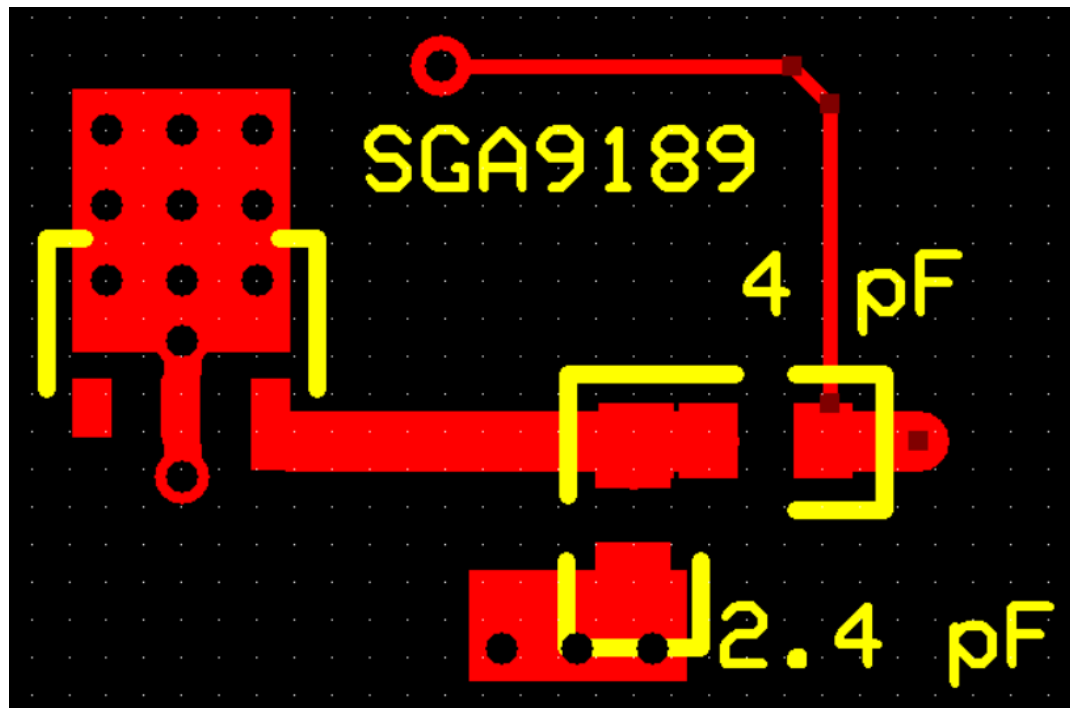
Type: Ind, Ind, Cap

Calculate Resonant Freq (GHz): 3.23

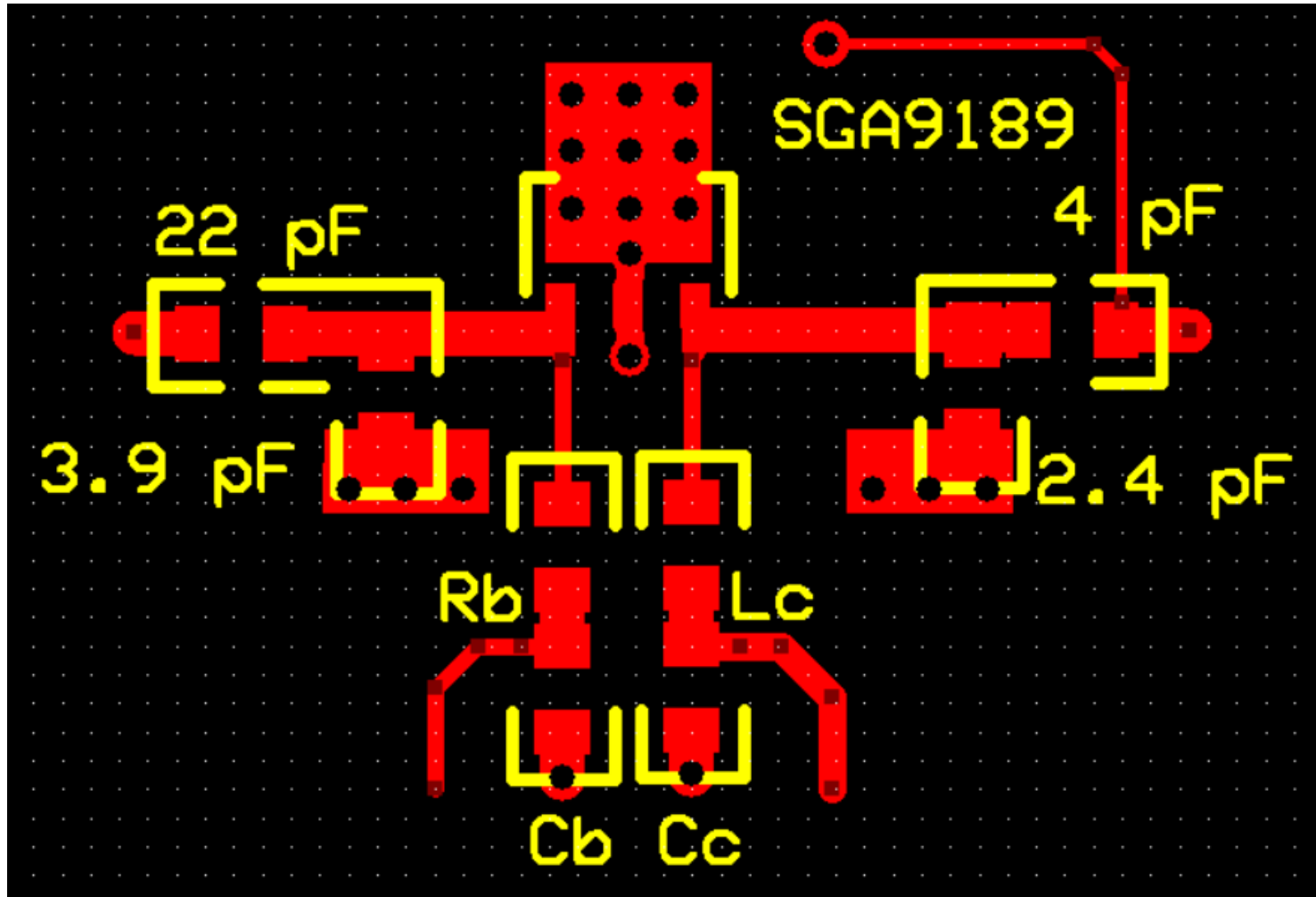
- SHUNT INDUCTOR
- PARALLEL LC EQUIVALENT
- EFFECTIVE INDUCTNCE = 10.3 nH



OUTPUT MATCH ON 50 MIL FR4



1296 MHz DRIVER LAYOUT WITH BIAS FEEDS



SOFTWARE TOOLS

- SMITH:

<http://www.fritz.dellsperger.net/smith.html>

- MICROSTRIP LUMPED EQUIVALENT:

<http://k5tra.net/TechFiles/LumpEquiv.exe>

- SERIES TRAP:

<http://k5tra.net/TechFiles/SeriesTrap.exe>

- SHUNT TRAP:

<http://k5tra.net/TechFiles/ShuntTrap.exe>